

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

## Tasks set examples for different simulation intervals

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Study Project, 2017

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

## Outline I

### 1 Leung and Merrill (1980)

- Interval Definition
- Set 1
- Set 2

### 2 Goossens and Devillers (1999)

- Interval Definition
- Set 1
- Set 2

### 3 Goossens and Devillers (1997)

- Interval Definition
- Set 1

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

## Outline II

- Set 2

### ④ Choquet-Geniet and Grolleau (2004), Bado et al. (2012)

- Interval Definition
- Set 1
- Set 2

### ⑤ Cucu and Goossens (2006)

- Interval Definition
- Set 1
- Set 2

### ⑥ Cucu-Grosjean and Goossens (2011)

- Interval Definition

- Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

## Outline III

- Set 1
- Set 2

### 7 Cucu and Goossens (2007)

- Interval Definition
- Set 1
- Set 2

### 8 Baro et al. (2012), Nélis et al. (2013)

- Interval Definition
- Set 1
- Set 2

### 9 Baro et al. (2012)

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

## Outline IV

- Interval Definition
- Set 1
- Set 2

### 10 Goossens-Grolleau-Cucu (2016)

- Interval Definition
- Set 1
- Set 2

- Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

## Leung and Merrill (1980)

### Interval Definition

Processor	1
Deadline	$D_i < T_i$
Dependency	Independent
Scheduling algorithm	Fixed-task priority
Simulation interval	$[0, O^{max} + 2H)$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

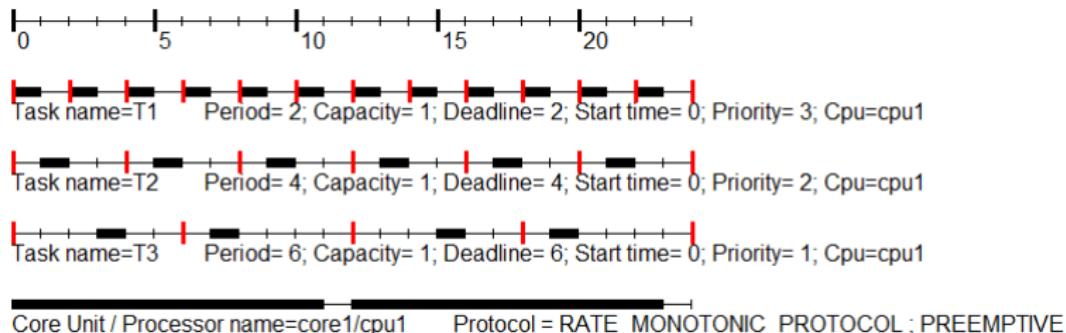
#### Interval Definition

Set 1

Set 2

## Leung and Merrill (1980)

Set 1



- $H = 12$
- Simulation interval in  $[0, 24]$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

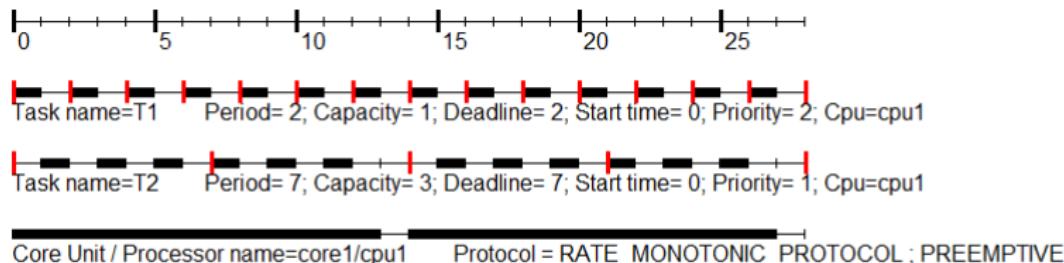
#### Interval Definition

Set 1

Set 2

## Leung and Merrill (1980)

Set 2



- $H = 14$
- Simulation interval in  $[0, 28)$

Leung and Merrill (1980)  
**Goossens and Devillers (1999)**  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

## Goossens and Devillers (1999)

### Interval Definition

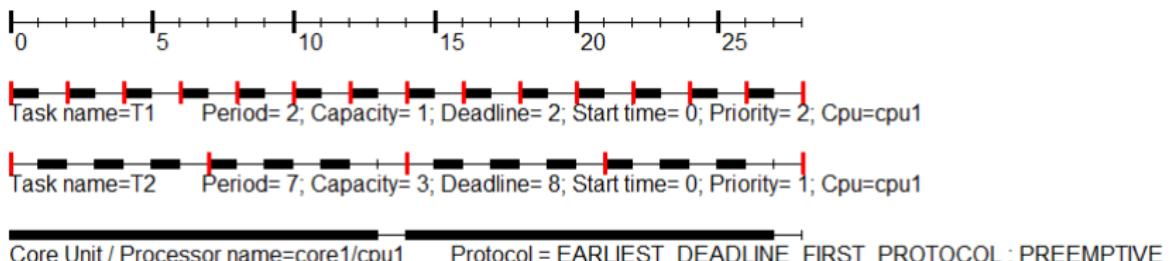
Processor	1
Deadline	Arbitrary
Dependency	Independent
Scheduling algorithm	Fixed-job priority
Simulation interval	$[0, O^{max} + 2H]$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

Interval Definition  
Set 1  
Set 2

## Goossens and Devillers (1999)

Set 1



- $H = 14$
- Simulation interval in  $[0, 28]$

Leung and Merrill (1980)  
**Goossens and Devillers (1999)**  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

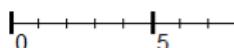
#### Interval Definition

Set 1

Set 2

## Goossens and Devillers (1999)

Set 2



Task name=T1      Period= 2; Capacity= 1; Deadline= 2; Start time= 0; Priority= 2; Cpu=cpu1

Task name=T2      Period= 4; Capacity= 3; Deadline= 5; Start time= 0; Priority= 1; Cpu=cpu1

Core Unit / Processor name=core1/cpu1      Protocol = EARLIEST\_DEADLINE\_FIRST\_PROTOCOL ; PREEMPTIVE

- $H = 4$
- Simulation interval in  $[0, 8)$
- $T_2$  missed its deadline at  $t=5$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
**Goossens and Devillers (1997)**  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

## Goossens and Devillers (1997)

### Interval Definition

Processor	1
Deadline	$D_i < T_i$
Dependency	Independent
Scheduling algorithm	Fixed-job priority
Simulation interval	$[0, S_n + H)$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
**Goossens and Devillers (1997)**  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

#### Interval Definition

Set 1

Set 2

## Goossens and Devillers (1997)

Set 1



Task name=T1      Period= 2; Capacity= 1; Deadline= 2; Start time= 0; Priority= 2; Cpu=cpu1

Task name=T2      Period= 4; Capacity= 1; Deadline= 4; Start time= 2; Priority= 1; Cpu=cpu1

Task name=T3      Period= 6; Capacity= 1; Deadline= 6; Start time= 3; Priority= 1; Cpu=cpu1

Core Unit / Processor name=core1/cpu1      Protocol = EARLIEST\_DEADLINE\_FIRST\_PROTOCOL ; PREEMPTIVE

- $H = 12$
- Simulation interval in  $[0, 15]$

## Goossens and Devillers (1997)

Set 1

- $S_1 = 0$

$$S_2 = \max\left(2, 2 + \left\lceil \frac{-2}{4} \right\rceil 4\right) = 2$$

$$S_3 = \max\left(3, 3 + \left\lceil \frac{2-3}{6} \right\rceil 6\right) = 3$$

$$S_3 + H = 15$$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
**Goossens and Devillers (1997)**  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

#### Interval Definition

Set 1

Set 2

## Goossens and Devillers (1997)

Set 2



Task name=T1      Period= 2; Capacity= 1; Deadline= 2; Start time= 0; Priority= 2; Cpu(cpu1)

Task name=T2      Period= 7; Capacity= 2; Deadline= 7; Start time= 3; Priority= 1; Cpu(cpu1)

Core Unit / Processor name=core1/cpu1      Protocol = EARLIEST\_DEADLINE\_FIRST\_PROTOCOL ; PREEMPTIVE

- $H = 14$
- Simulation interval in  $[0, 17)$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
**Goossens and Devillers (1997)**  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

Interval Definition

Set 1

Set 2

## Goossens and Devillers (1997)

Set 2

- $S_1 = 0$

$$S_2 = \max\left(3, 3 + \left\lceil \frac{-3}{7} \right\rceil 7\right) = 3$$

$$S_2 + H = 17$$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
**Choquet-Geniet and Grolleau (2004), Bado et al. (2012)**  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

## Choquet-Geniet and Grolleau (2004), Bado et al. (2012)

### Interval Definition

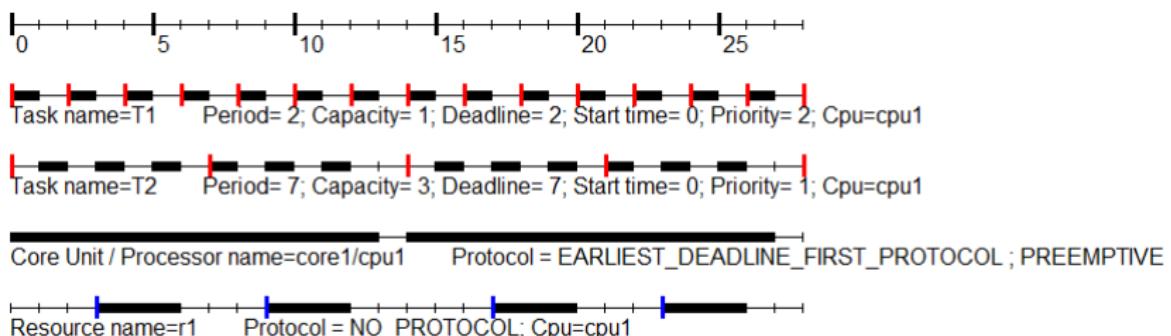
Processor	1
Deadline	$D_i < T_i$
Dependency	Mutual Exclusion, Simple precedence
Scheduling algorithm	Any work-conserving ( <i>with idle task</i> )
Simulation interval	$[0, \theta_c + H)$

- Leung and Merrill (1980)  
 Goossens and Devillers (1999)  
 Goossens and Devillers (1997)  
**Choquet-Geniet and Grolleau (2004), Bado et al. (2012)**  
 Cucu and Goossens (2006)  
 Cucu-Grosjean and Goossens (2011)  
 Cucu and Goossens (2007)  
 Baro et al. (2012), Nélis et al. (2013)  
 Baro et al. (2012)  
 Goossens-Grolleau-Cucu (2016)

Interval Definition  
 Set 1  
 Set 2

## Choquet-Geniet and Grolleau (2004), Bado et al. (2012)

Set 1



Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
**Choquet-Geniet and Grolleau (2004), Bado et al. (2012)**  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

Interval Definition

Set 1

Set 2

## Choquet-Geniet and Grolleau (2004), Bado et al. (2012)

Set 1

- $H = 14$
- T2 accesses to R1 during 2 u.t from it's 2<sup>nd</sup> to it's 3<sup>rd</sup> u.t
- Simulation interval in  $[0, 28]$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
**Choquet-Geniet and Grolleau (2004), Bado et al. (2012)**  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

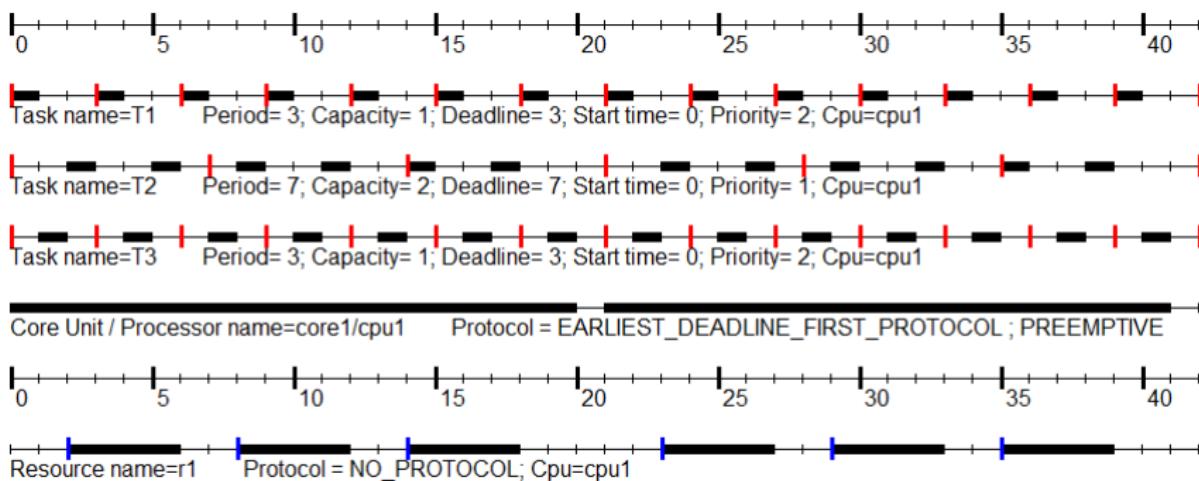
#### Interval Definition

**Set 1**

**Set 2**

## Choquet-Geniet and Grolleau (2004), Bado et al. (2012)

Set 2



Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
**Choquet-Geniet and Grolleau (2004), Bado et al. (2012)**  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

Interval Definition

Set 1

Set 2

## Choquet-Geniet and Grolleau (2004), Bado et al. (2012)

Set 2

- $H = 14$
- T2 accesses to R1 during 2 u.t from it's 1<sup>st</sup> to it's 2<sup>nd</sup> u.t
- Simulation interval in  $[0, 42]$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
**Cucu and Goossens (2006)**  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

## Cucu and Goossens (2006)

### Interval Definition

Processor	Uniform
Deadline	$D_i < T_i$
Dependency	Independent
Scheduling algorithm	Global fixed-task priority)
Simulation interval	$S_n + H$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
**Cucu and Goossens (2006)**  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

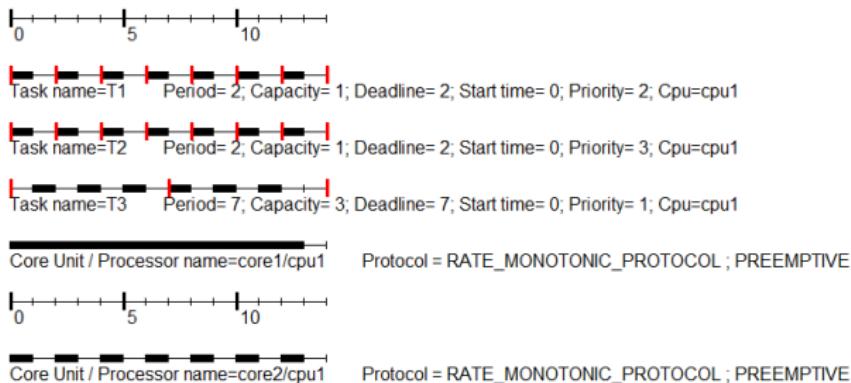
#### Interval Definition

Set 1

Set 2

## Cucu and Goossens (2006)

Set 1



- $H = 14$ , Simulation interval in  $[0, 14]$

- Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
**Cucu and Goossens (2006)**  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

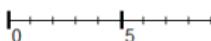
#### Interval Definition

Set 1

Set 2

## Cucu and Goossens (2006)

Set 2

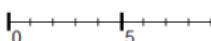


Task name=T1    Period= 4; Capacity= 1; Deadline= 4; Start time= 1; Priority= 1; Cpu(cpu1)

Task name=T2    Period= 4; Capacity= 3; Deadline= 4; Start time= 0; Priority= 2; Cpu(cpu1)

Task name=T3    Period= 4; Capacity= 4; Deadline= 4; Start time= 4; Priority= 3; Cpu(cpu1)

Core Unit / Processor name=core1/cpu1    Protocol = RATE\_MONOTONIC\_PROTOCOL ; PREEMPTIVE



Core Unit / Processor name=core2/cpu1    Protocol = RATE\_MONOTONIC\_PROTOCOL ; PREEMPTIVE

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
**Cucu and Goossens (2006)**  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

## Cucu and Goossens (2006)

Set 2

- $H = 4$
- $S_3 = 4$

$$S_2 = \max\left(0, 0 + \left\lceil \frac{4}{4} \right\rceil 4\right) = 4$$

$$S_1 = \max\left(1, 1 + \left\lceil \frac{4-1}{4} \right\rceil 4\right) = 5$$

$$S_1 + H = 9$$

- Simulation interval in  $[0, 9)$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
**Cucu-Grosjean and Goossens (2011)**  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

## Cucu-Grosjean and Goossens (2011)

### Interval Definition

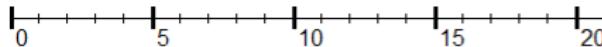
Processor	Unrelated
Deadline	$D_i < T_i$
Dependency	Independent
Scheduling algorithm	Global fixed-task priority)
Simulation interval	$S_n + H$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
**Cucu-Grosjean and Goossens (2011)**  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

Interval Definition  
Set 1  
Set 2

## Cucu-Grosjean and Goossens (2011)

Set 1

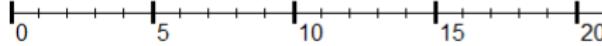


Task name=T1      Period= 2; Capacity= 1; Deadline= 2; Start time= 0; Priority= 2; Cpu=cpu1

Task name=T2      Period= 2; Capacity= 1; Deadline= 2; Start time= 5; Priority= 3; Cpu=cpu1

Task name=T3      Period= 7; Capacity= 3; Deadline= 7; Start time= 0; Priority= 1; Cpu=cpu1

Core Unit / Processor name=core1/cpu1      Protocol = DEADLINE\_MONOTONIC\_PROTOCOL ; PREEMPTIVE



Core Unit / Processor name=core2/cpu1      Protocol = DEADLINE\_MONOTONIC\_PROTOCOL ; PREEMPTIVE

Leung and Merrill (1980)
Goossens and Devillers (1999)
Goossens and Devillers (1997)
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)
Cucu and Goossens (2006)
<b>Cucu-Grosjean and Goossens (2011)</b>
Cucu and Goossens (2007)
Baro et al. (2012), Nélis et al. (2013)
Baro et al. (2012)
Goossens-Grolleau-Cucu (2016)

Interval Definition

Set 1

Set 2

## Cucu-Grosjean and Goossens (2011)

Set 1

- $H = 14$
- $S_2 = 5$

$$S_1 = \max\left(0, 0 + \left\lceil \frac{5}{2} \right\rceil 2\right) = 6$$

$$S_3 = \max\left(0, 0 + \left\lceil \frac{6}{7} \right\rceil 7\right) = 7$$

$$S_3 + H = 21$$

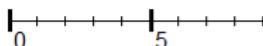
- Simulation interval in  $[0, 21)$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
**Cucu-Grosjean and Goossens (2011)**  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

Interval Definition  
Set 1  
Set 2

## Cucu-Grosjean and Goossens (2011)

Set 2

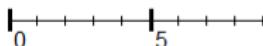


Task name=T1      Period= 4; Capacity= 1; Deadline= 4; Start time= 1; Priority= 1; Cpu(cpu1)

Task name=T2      Period= 4; Capacity= 3; Deadline= 4; Start time= 0; Priority= 2; Cpu(cpu1)

Task name=T3      Period= 4; Capacity= 4; Deadline= 4; Start time= 1; Priority= 3; Cpu(cpu1)

Core Unit / Processor name=core1/cpu1      Protocol = DEADLINE\_MONOTONIC\_PROTOCOL ; PREEMPTIVE



Core Unit / Processor name=core2/cpu1      Protocol = DEADLINE\_MONOTONIC\_PROTOCOL ; PREEMPTIVE

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
**Cucu-Grosjean and Goossens (2011)**  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

## Cucu-Grosjean and Goossens (2011)

Set 2

- $H = 4$
- $S_3 = 1$

$$S_2 = \max\left(0, 0 + \left\lceil \frac{1}{4} \right\rceil 4\right) = 4$$

$$S_1 = \max\left(1, 1 + \left\lceil \frac{4-1}{4} \right\rceil 4\right) = 5$$

$$S_1 + H = 9$$

- Simulation interval in  $[0, 9)$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
**Cucu and Goossens (2007)**  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

## Cucu and Goossens (2007)

### Interval Definition

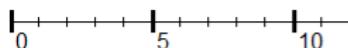
Processor	Identical
Deadline	Arbitrary
Dependency	Independent
Scheduling algorithm	Global fixed-task priority
Simulation interval	$[0, \hat{S}_n + H)$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
**Cucu and Goossens (2007)**  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

Interval Definition  
Set 1  
Set 2

## Cucu and Goossens (2007)

Set 1



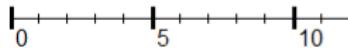
Task name=T1      Period= 2; Capacity= 1; Deadline= 2; Start time= 2; Priority= 2; Cpu=cpu1

Task name=T2      Period= 2; Capacity= 1; Deadline= 2; Start time= 0; Priority= 3; Cpu=cpu1

Task name=T3      Period= 4; Capacity= 3; Deadline= 7; Start time= 4; Priority= 1; Cpu=cpu1

Core Unit / Processor name=core1/cpu1

Protocol = DEADLINE\_MONOTONIC\_PROTOCOL ; PREEMPTIVE



Core Unit / Processor name=core2/cpu1

Protocol = DEADLINE\_MONOTONIC\_PROTOCOL ; PREEMPTIVE

Leung and Merrill (1980)
Goossens and Devillers (1999)
Goossens and Devillers (1997)
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)
Cucu and Goossens (2006)
Cucu-Grosjean and Goossens (2011)
<b>Cucu and Goossens (2007)</b>
Baro et al. (2012), Nélis et al. (2013)
Baro et al. (2012)
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

## Cucu and Goossens (2007)

Set 1

- $H = 4$
- Simulation interval in  $[0, 12)$
- $\hat{S}_2 = 0$

$$\hat{S}_1 = \max\left(2, 2 + \left\lceil \frac{-2}{2} \right\rceil 2\right) + 2 = 4$$

$$\hat{S}_3 = \max(4, 4) + 4 = 8$$

$$\hat{S}_3 + H = 12$$

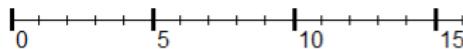
- Simulation interval in  $[0, 12)$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
**Cucu and Goossens (2007)**  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

Interval Definition  
Set 1  
Set 2

## Cucu and Goossens (2007)

Set 2

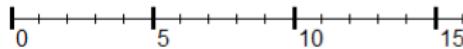


Task name=T1      Period= 4; Capacity= 1; Deadline= 4; Start time= 1; Priority= 2; Cpu=cpu1

Task name=T2      Period= 4; Capacity= 2; Deadline= 5; Start time= 0; Priority= 1; Cpu=cpu1

Task name=T3      Period= 4; Capacity= 4; Deadline= 4; Start time= 0; Priority= 3; Cpu=cpu1

Core Unit / Processor name=core1/cpu1      Protocol = DEADLINE\_MONOTONIC\_PROTOCOL ; PREEMPTIVE



Core Unit / Processor name=core2/cpu1      Protocol = DEADLINE\_MONOTONIC\_PROTOCOL ; PREEMPTIVE

Leung and Merrill (1980)
Goossens and Devillers (1999)
Goossens and Devillers (1997)
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)
Cucu and Goossens (2006)
Cucu-Grosjean and Goossens (2011)
<b>Cucu and Goossens (2007)</b>
Baro et al. (2012), Nélis et al. (2013)
Baro et al. (2012)
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

## Cucu and Goossens (2007)

Set 2

- $H = 4$
- $\hat{S}_3 = 0$

$$\hat{S}_1 = \max\left(1, 1 + \left\lceil \frac{-1}{4} \right\rceil 4\right) + 4 = 5$$

$$\hat{S}_2 = \max\left(0, 0 + \left\lceil \frac{5}{4} \right\rceil 4\right) + 4 = 12$$

$$\hat{S}_2 + H = 16$$

- Simulation interval in  $[0, 16)$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

#### Interval Definition

Set 1

Set 2

Baro et al. (2012), Nélis et al. (2013)

Interval Definition

Processor	Identical
Deadline	$D_i < T_i$
Dependency	Independent
Scheduling algorithm	Any
Simulation interval	$[0, O^{max} + H \prod_{i=1}^n (C_i + 1))$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

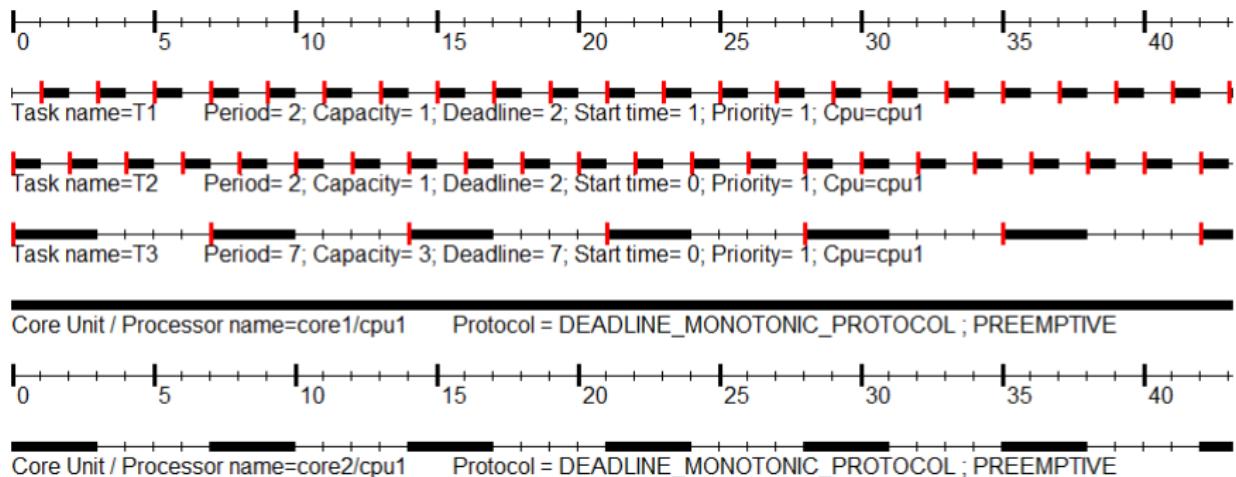
#### Interval Definition

Set 1

Set 2

## Baro et al. (2012), Nélis et al. (2013)

Set 1



Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

Interval Definition

Set 1

Set 2

## Baro et al. (2012), Nélis et al. (2013)

Set 1

- $H = 14, O^{max} = 1$
- $1 + 14 \times (2 \times 2 \times 7)$   
 $= 225$
- Simulation interval in  $[0, 225]$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

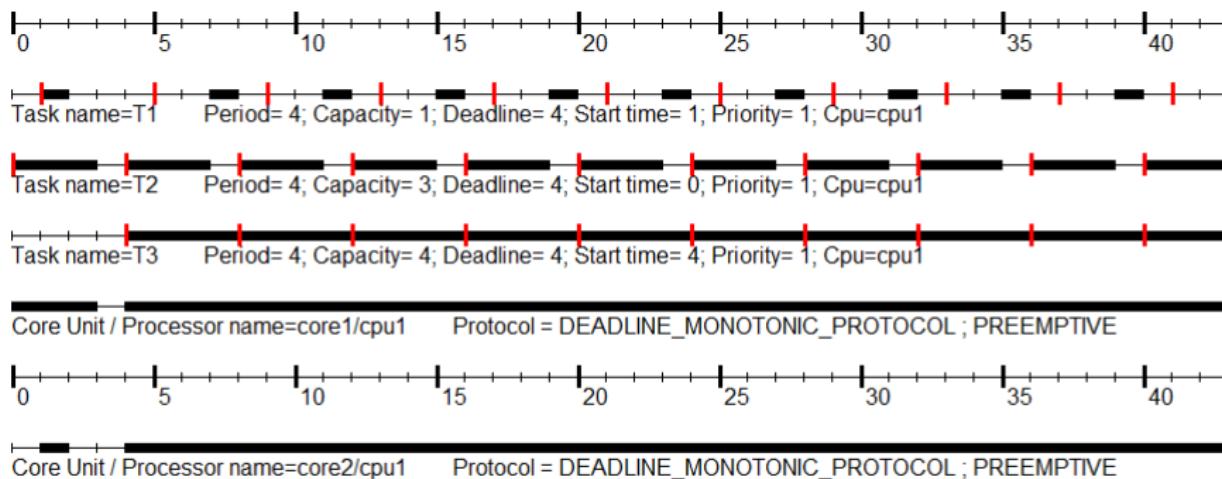
#### Interval Definition

Set 1

Set 2

## Baro et al. (2012), Nélis et al. (2013)

Set 2



Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

Baro et al. (2012), Nélis et al. (2013)

Set 2

- $H = 4, O^{max} = 4$
- $4 + 4 \times 40$   
 $= 164$
- Simulation interval in  $[0, 164)$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
**Baro et al. (2012)**  
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

## Baro et al. (2012)

### Interval Definition

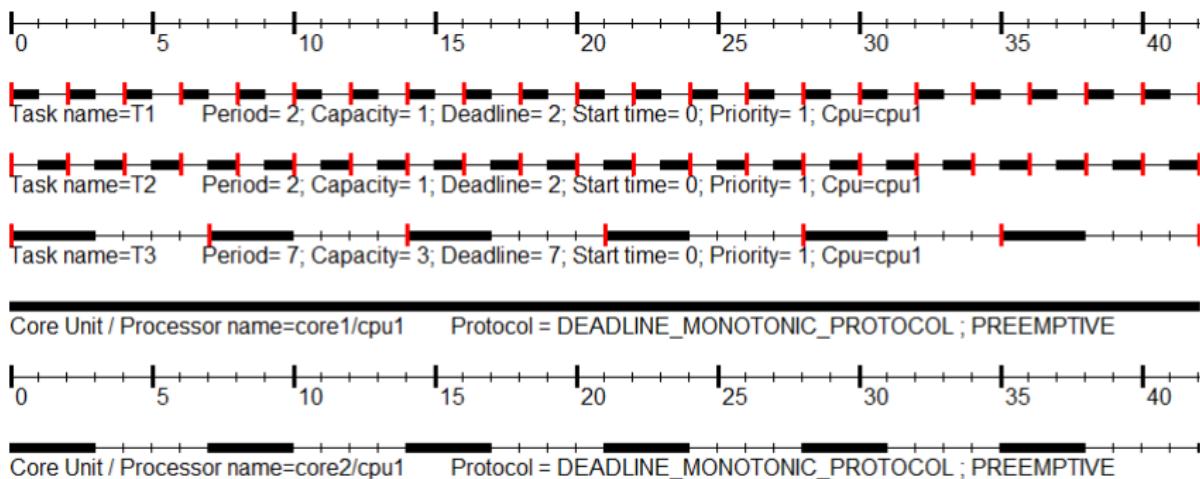
Processor	Identical
Deadline	$D_i < T_i$
Dependency	Simple precedence
Scheduling algorithm	Any
Simulation interval	$[0, O^{max} + H \prod_{i=1}^n (C_i + 1))$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
**Baro et al. (2012)**  
Goossens-Grolleau-Cucu (2016)

Interval Definition  
Set 1  
Set 2

## Baro et al. (2012)

Set 1



Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
**Baro et al. (2012)**  
Goossens-Grolleau-Cucu (2016)

Interval Definition

Set 1

Set 2

## Baro et al. (2012)

Set 1

- $H = 14, O^{max} = 0$
- $4 \times (2 \times 2 \times 4) = 224$
- Simulation interval in  $[0, 224)$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
**Baro et al. (2012)**  
Goossens-Grolleau-Cucu (2016)

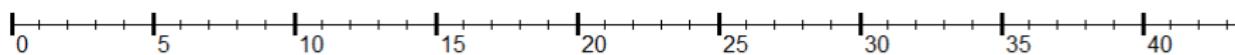
#### Interval Definition

Set 1

Set 2

## Baro et al. (2012)

Set 2

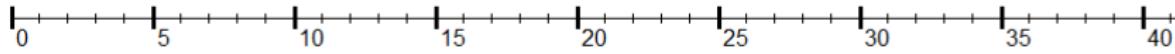


Task name=T1      Period= 4; Capacity= 1; Deadline= 4; Start time= 0; Priority= 1; Cpu=cpu1

Task name=T2      Period= 4; Capacity= 1; Deadline= 4; Start time= 0; Priority= 1; Cpu=cpu1

Task name=T3      Period= 6; Capacity= 1; Deadline= 6; Start time= 0; Priority= 1; Cpu=cpu1

Core Unit / Processor name=core1/cpu1      Protocol = DEADLINE\_MONOTONIC\_PROTOCOL ; PREEMPTIVE



Core Unit / Processor name=core2/cpu1      Protocol = DEADLINE\_MONOTONIC\_PROTOCOL ; PREEMPTIVE

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
**Baro et al. (2012)**  
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

## Baro et al. (2012)

Set 2

- $H = 12, O^{max} = 0$
- $12 \times 2^3 = 96$
- Simulation interval in  $[0, 96)$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

## Goossens-Grolleau-Cucu (2016)

### Interval Definition

Processor	Identical
Deadline	$D_i < T_i$
Dependency	Simple precedence
Scheduling algorithm	Any
Simulation interval	$[0, H \prod_{i=1}^n ((O_i + D_i - T_i)_0 + 1))$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

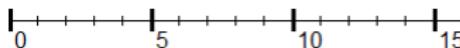
#### Interval Definition

Set 1

Set 2

## Goossens-Grolleau-Cucu (2016)

Set 1



Task name=T1      Period= 2; Capacity= 1; Deadline= 2; Start time= 0; Priority= 1; Cpu=cpu1

Task name=T2      Period= 2; Capacity= 1; Deadline= 2; Start time= 0; Priority= 1; Cpu=cpu1

Task name=T3      Period= 4; Capacity= 3; Deadline= 7; Start time= 0; Priority= 1; Cpu=cpu1

Core Unit / Processor name=core1/cpu1      Protocol = EARLIEST\_DEADLINE\_FIRST\_PROTOCOL ; PREEMPTIVE



Core Unit / Processor name=core2/cpu1      Protocol = EARLIEST\_DEADLINE\_FIRST\_PROTOCOL ; PREEMPTIVE

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

Interval Definition

Set 1

Set 2

## Goossens-Grolleau-Cucu (2016)

Set 1

- $H = 4$ ,
- Simulation interval in  $[0, 16]$

Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

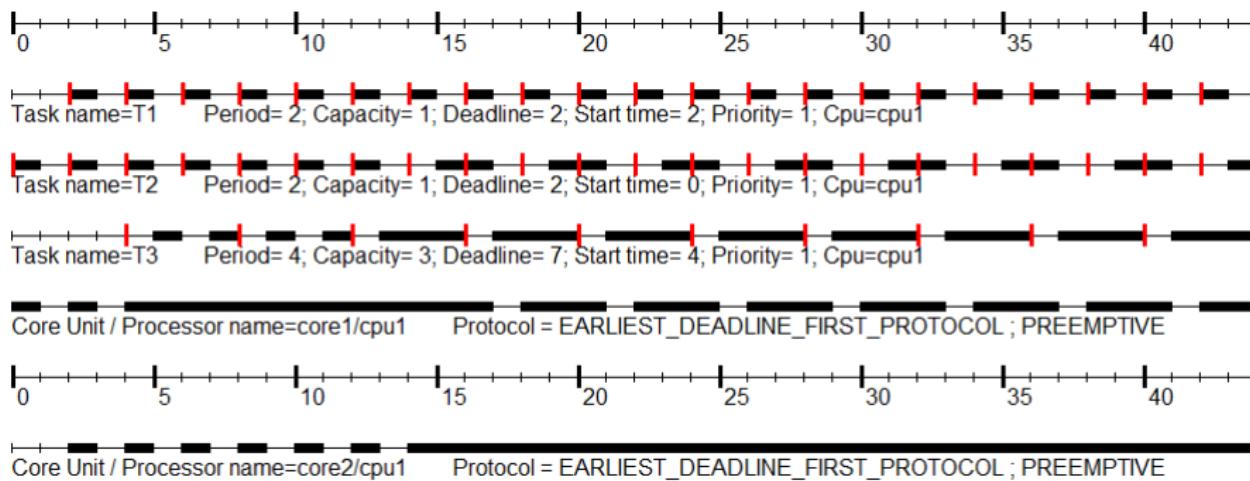
#### Interval Definition

Set 1

Set 2

## Goossens-Grolleau-Cucu (2016)

Set 2



Leung and Merrill (1980)  
Goossens and Devillers (1999)  
Goossens and Devillers (1997)  
Choquet-Geniet and Grolleau (2004), Bado et al. (2012)  
Cucu and Goossens (2006)  
Cucu-Grosjean and Goossens (2011)  
Cucu and Goossens (2007)  
Baro et al. (2012), Nélis et al. (2013)  
Baro et al. (2012)  
Goossens-Grolleau-Cucu (2016)

### Interval Definition

Set 1

Set 2

## Goossens-Grolleau-Cucu (2016)

Set 2

- $H = 4$ ,
- $(3 \times 1 \times 8)4$   
 $= 96$
- Simulation interval in  $[0, 96]$